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VECTOR VALUED FOURIER ANALYSIS ON HYPERGROUPS

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Abstract. The aim of this paper is to prove the vector-valued version of the classical Hausdorff-Young inequality for commutative hypergroups and compact hypergroups.

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