

INVARIANCE OF DISTRIBUTIONAL CHAOS FOR BACKWARD SHIFTS

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Abstract. A sufficient and necessary condition ensuring that the backward shift operator on the Köthe sequence space admits an invariant distributionally ε -scrambled set for some $\varepsilon > 0$ is obtained, improving the main results in [10].

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