

## ASYMPTOTIC STABILITY OF A PERTURBED ABSTRACT DIFFERENTIAL EQUATIONS IN BANACH SPACES

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*Abstract.* This paper is mainly concerned with the asymptotic stability of the solutions of a perturbed abstract differential equation in Banach spaces. Let  $A$  be a generator of an exponentially stable operator semigroup and let  $C(t)$ ,  $t \geq 0$  be a linear bounded variable operator. Assuming that the perturbation  $F(t, x)$  is sufficiently small norm for the equation  $\frac{dx}{dt} = Ax + C(t)x + F(t, x)$ , we derive the Lyapunov asymptotic stability conditions. These results are applied to partial differential equations.

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