

## ON THE NUMERICAL RANGE AND OPERATOR NORM OF $V^2$

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*Abstract.* Let  $V$  denote the classical Volterra operator on  $L^2(0, 1)$ . We investigate the numerical range and operator norm of  $V^2$ . In particular, we obtain the numerical range, numerical radius and norm of  $\operatorname{Re}V^2$  and  $\operatorname{Im}V^2$ .

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