

## ON THE NORM OF HANKEL OPERATOR RESTRICTED TO FOCK SPACE

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*Abstract.* In this note, we characterize the norm of Hankel operator  $H_{\bar{z}}$ . Then we find the formula of the norm of  $H_{\bar{z}^n}(g)$  and give an upper bound of the norm of  $H_n$  on Fock space. Lastly, we prove the concomitant operator  $P_n$  of  $H_{\bar{z}^n}$  is quasi-affine to the direct sum of  $n$  copies of the concomitant operator  $P_1$  of  $H_{\bar{z}}$ .

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