

## COMMUTATIVITY OF TOEPLITZ OPERATORS ON THE BERGMAN SPACES OF THE UNIT DISK

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*Abstract.* In this paper we give some necessary and sufficient conditions that Toeplitz operators with special symbols commute with Toeplitz operators with harmonic symbols on the Bergman space.

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