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UNCERTAINTY PRINCIPLES IN TERM OF SUPPORTS IN HANKEL WAVELET SETTING

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Abstract. Uncertainty principles in term of supports, namely Amrein-Berthier and Logvinenko-Sereda theorems are proved for the continuous Hankel wavelet transform.

Mathematics subject classification (2020): 42A38, 35S30, 42B10.
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