

## DETERMINANTAL POLYNOMIALS OF A WEIGHTED SHIFT MATRIX WITH PALINDROMIC GEOMETRIC WEIGHTS

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*Abstract.* We find an explicit expression of the determinantal polynomials of a weighted shift matrix with palindromic geometric weights.

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