

ON A GENERALIZATION OF LEFT AND RIGHT INVERTIBLE OPERATORS ON BANACH SPACES

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Abstract. The purpose of this paper is to define and study left and right versions of the large class of Drazin invertible operators on Banach spaces, namely left and right Drazin invertible operators, as a generalization of left and right invertible operators. It is shown in particular that the operators introduced can be characterized by means of Kato decompositions.

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