

ON n -LIE DERIVATIONS OF TRIANGULAR ALGEBRAS

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Abstract. This article is about the study of n -Lie derivations on triangular algebras under certain restrictions and it is shown that every n -Lie derivation apparently split into an extremal n -derivation and an n -linear central map on triangular algebras. In addition, we implement this result to the classical examples of triangular algebras.

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