

ATOMIC LATTICES OF SUBSPACES OF AN ARBITRARY VECTOR SPACE AND ASSOCIATED OPERATOR ALGEBRAS

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Abstract. We study a class of completely distributive, commutative, lattices of subspaces of an arbitrary vector space, and associated operator algebras. Our results are compared with corresponding results for commutative lattices of closed subspaces of a Hilbert space and associated algebras of bounded linear operators.

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