

ISOLATION AMONGST COMPOSITION OPERATORS ON $L^p(\mu)$ -SPACES ($1 \leq p \leq \infty$)

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Abstract. In this paper we show that each composition operator is isolated in $\text{comp}(L^p)$ ($1 \leq p \leq \infty$) under the norm topology. We also prove that while each composition operator is non-isolated in $\text{comp}(L^p)$ ($1 \leq p < \infty$) under the strong operator topology, every composition operator is isolated in $\text{comp}(L^\infty)$ under the strong operator topology.

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