

BIRKHOFF–JAMES ORTHOGONALITY IN CERTAIN TENSOR PRODUCTS OF BANACH SPACES

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Abstract. In this article, the relationship between Birkhoff-James orthogonality of elementary tensors in certain tensor product spaces with the Birkhoff-James orthogonality of individual elements in their respective spaces is studied.

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