

FURTHER REFINEMENTS OF SOME NUMERICAL RADIUS INEQUALITIES FOR OPERATORS

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Abstract. In this work, we give refinements of some well-known numerical radius inequalities. Also, we present an improvement of the triangle inequality for the operator norm.

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