

## LOG-MAJORIZATION OF GAN-LIU-TAM TYPE

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*Abstract.* In this paper, we shall obtain several extensions of log-majorization of Gan-Liu-Tam type.

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