

INVERTIBLE ELEMENTS AND COMMUTATIVITY IN BANACH ALGEBRAS

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Abstract. This paper investigates the commutativity of Banach algebras in which the group of invertible elements is subject to certain algebraic and metric conditions. Application to a particular class of Banach algebras is examined.

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