

IDEALS IN HAAGERUP TENSOR PRODUCT OF C^* -TERNARY RINGS AND TROS

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Abstract. We characterize the maximal, prime and primitive ideals of Haagerup tensor product $M \otimes^h B$ of a TRO M and a C^* -algebra B .

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