

SOME INEQUALITIES FOR EIGENVALUES AND POSITIVE LINEAR MAPS

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Abstract. In this paper, we demonstrate some inequalities for positive linear maps on matrices. Moreover, we discuss lower bounds for the spread of nonnegative matrices which provides improvement over the existing bounds.

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