

q -NUMERICAL RADIUS INEQUALITIES FOR PRODUCT OF COMPLEX LINEAR BOUNDED OPERATORS

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Abstract. In this paper, we prove some q -numerical radius power inequalities for a product of operators on a complex Hilbert space. We introduce also the notion of the q -center for bounded operators, and we give the relationship between this q -center, the q -numerical radius and the center of the q -numerical range.

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